# Discrete Mathematics 

## Lecture 01

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Faculty of Computers and Artificial Intelligence

## Benha University

Spring 2023

## Introduce Myself

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## Basic Course Information

- Course code: FBS102-NBS102
- Course name: Discrete Mathematics
- Level: $1^{\text {st }}$ Year / B.Sc.
- Course Credit: $\mathbf{3}$ credits
- Instructor: Dr. Ahmed Hagag


## Assessment



## Lectures Reference

## كلية الحاسبات والذكاء الإصطناعي



## Textbook 2019

https://drive.google.com/drive/folders/1 a2rpYLZtEzuTyRZVqkN1mAnvIATd1dq6?u sp=sharing


## Discussion Question

## Why do we study this course?

## Course Objectives

- Learn how to think mathematically.
- Grasp the basic logical and reasoning mechanisms of mathematical thought.
- Acquire logic and proof as the basics for abstract thinking.
- Improve problem-solving skills.
- Grasp the basic elements of induction, recursion, combination and discrete structures.


## DM is a Gateway Course

Topics in discrete mathematics will be important in many courses that you will take in the future:

- Computer Science: Computer Architecture, Data Structures, Algorithms, Programming Languages, Compilers, Computer Security, Databases, Artificial Intelligence, Networking, Graphics, Game Design, Theory of Computation, ......
- Mathematics: Logic, Set Theory, Probability, Number Theory, Abstract Algebra, Combinatorics, Graph Theory, Game Theory, Network Optimization, ...
- Other Disciplines: You may find concepts learned here useful in courses in philosophy, economics, linguistics, and other departments.


## Course Syllabus

## Some topics from the following chapters:

- The Foundations: Logic and Proofs.
- Basic Structures: Sets, Functions, Sequences, and Sums.
- Algorithms.
- Number Theory and Cryptography.
- Induction and Recursion.
- Relations.
- Graphs.
- Trees.


## Chapter 1: Logic and Proofs

## Some topics from the following sections:

- Introduction to Propositional Logic.
- Compound Propositions.
- Applications of Propositional Logic.
- Propositional Equivalences.
- Predicates and Quantifiers.
- Nested Quantifiers
- Rules of Inference.
- Introduction to Proofs.


## Introduction to Propositional Logic (1/4)

## What is Logic?

- Logic is the discipline that deals with the methods of reasoning.
- On an elementary level, logic provides rules and techniques for determining whether a given argument is valid.
- Logical reasoning is used in mathematics to prove theorems.


## Introduction to Propositional Logic (2/4)

- The basic building blocks of logic is Proposition
- A proposition (or statement) is a declarative sentence that is either true or false, but not both.
- The area of logic that deals with propositions is called propositional logics.



## Introduction to Propositional Logic (3/4)

## كلية الحاسبات والذكاء الإصطناعي

## Examples:

| Propositions | Truth value |
| :---: | :---: |
| $2+3=5$ | True |
| $5-2=1$ | False |
| Today is Friday | False |
| $x+3=7, \quad$ for $x=4$ | True |
| Cairo is the capital of Egypt | True |


| Sentences | Is a Proposition |
| :---: | :---: |
| What time is it? | Not propositions |
| Read this carefully. | Not propositions |
| $x+3=7$ | Not propositions |

## Introduction to Propositional Logic (4/4)

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- We use letters to denote propositional variables $p, q, r, s, \ldots$
- The truth value of a proposition is true, denoted by $T$, if it is a true proposition and false, denoted by $\mathbf{F}$, if it is a false proposition.


## Compound Propositions (1/23)

## Compound Proposition

- Compound Propositions are formed from existing propositions using logical operators.



## Compound Propositions (2/23)

## كلية الحاسبات والذكاء الإصطناعي

## Negation

## DEFINITION 1

Let $p$ be a proposition. The negation of $p$, denoted by $\neg p($ also denoted by $\bar{p})$, is the statement "It is not the case that $p$."

The proposition $\neg p$ is read "not $p$." The truth value of the negation of $p, \neg p$, is the opposite of the truth value of $p$.

Other notations you might see are $\sim p,-p, p^{\prime}, \mathrm{N} p$, and $!p$.

## Compound Propositions (3/23)

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## Example

Find the negation of the proposition
p: "Cairo is the capital of Egypt"

## Compound Propositions (4/23)

## Example: Solution

Find the negation of the proposition
p: "Cairo is the capital of Egypt"
The negation is
$\neg p$ : "It is not the case that Cairo is the capital of Egypt"
This negation can be more simply expressed as
$\neg p$ : "Cairo is not the capital of Egypt"

## Compound Propositions (5/23)

## Truth Table

- Truth Table: is a table that gives the truth values of a compound statement.

The Truth Table for the Negation of a Proposition


## Compound Propositions (5/23)

## Truth Table

- Truth Table: is a table that gives the truth values of a compound statement.

The Truth Table for the Negation of a Proposition


## Compound Propositions (6/23)

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## Negation

## TABLE 1 The Truth Table for the Negation of a Proposition.

| $\boldsymbol{p}$ | $\neg \boldsymbol{p}$ |
| :---: | :---: |
| T | F |
| F | T |

## Compound Propositions (7/23)

## Logical Connectives

## DEFINITION 2

Let $p$ and $q$ be propositions. The conjunction of $p$ and $q$, denoted by $p \wedge q$, is the proposition " $p$ and $q$." The conjunction $p \wedge q$ is true when both $p$ and $q$ are true and is false otherwise.

## Example

$p: \quad$ Today is Friday.
$q$ : It is raining today.
$p \wedge q$ : Today is Friday and it is raining today.

TABLE 2 The Truth Table for the Conjunction of Two Propositions.

| $\boldsymbol{p}$ | $\boldsymbol{q}$ | $\boldsymbol{p} \wedge \boldsymbol{q}$ |
| :---: | :---: | :---: |
| T | T | T |
| T | F | F |
| F | T | F |
| F | F | F |

## Compound Propositions (8/23)

## Logical Connectives

## DEFINITION 3

Let $p$ and $q$ be propositions. The disjunction of $p$ and $q$, denoted by $p \vee q$, is the proposition " $p$ or $q$." The disjunction $p \vee q$ is false when both $p$ and $q$ are false and is true otherwise.

## Example

$p: \quad$ Today is Friday.
$q: \quad$ It is raining today.
$p \vee q$ : Today is Friday or it is raining today.

TABLE 3 The Truth Table for the Disjunction of Two Propositions.

| $\boldsymbol{p}$ | $\boldsymbol{q}$ | $\boldsymbol{p} \vee \boldsymbol{q}$ |
| :---: | :---: | :---: |
| T | T | T |
| T | F | T |
| F | T | T |
| F | F | F |

## Compound Propositions (9/23)

## Logical Connectives

## DEFINITION 4

Let $p$ and $q$ be propositions. The exclusive or of $p$ and $q$, denoted by $p \oplus q$ (or $p \mathrm{XOR} q$ ), is the proposition that is true when exactly one of $p$ and $q$ is true and is false otherwise.

## Example

$p$ : They are parents.
$q$ : They are children.
$p \oplus q$ : They are parents or children but not both.

TABLE 4 The Truth Table for the Exclusive Or of Two Propositions.

| $\boldsymbol{p}$ | $\boldsymbol{q}$ | $\boldsymbol{p} \oplus \boldsymbol{q}$ |
| :---: | :---: | :---: |
| T | T | F |
| T | F | T |
| F | T | T |
| F | F | F |

## Compound Propositions (10/23)

## Logical Connectives

## DEFINITION 5

Let $p$ and $q$ be propositions. The conditional statement $p \rightarrow q$ is the proposition "if $p$, then $q$." The conditional statement $p \rightarrow q$ is false when $p$ is true and $q$ is false, and true otherwise. In the conditional statement $p \rightarrow q, p$ is called the hypothesis (or antecedent or premise) and $q$ is called the conclusion (or consequence).
"if $p$, then $q$ "
"if $p, q$ "
" $p$ is sufficient for $q$ "
" $q$ if $p$ "
" $q$ when $p$ "
"a necessary condition for $p$ is $q$ " " $q$ unless $\neg p$ "

| TABLE 5 The Truth Table for the Conditional Statement$p \rightarrow q .$ |  |  |
| :---: | :---: | :---: |
| $p$ | $q$ | $p \rightarrow q$ |
| T | T | T |
| T | F | F |
| F | T | T |
| F | F | T |

" $p$ implies $q$ "
" $p$ only if $q$ "
"a sufficient condition for $q$ is $p$ "
" $q$ whenever $p$ "
" $q$ is necessary for $p$ "
" $q$ follows from $p$ "

## Compound Propositions (10/23)

## Logical Connectives

## DEFINITION 5

Let $p$ and $q$ be propositions. The conditional statement $p \rightarrow q$ is the proposition "if $p$, then $q$." The conditional statement $p \rightarrow q$ is false when $p$ is true and $q$ is false, and true otherwise. In the conditional statement $p \rightarrow q, p$ is called the hypothesis (or antecedent or premise) and $q$ is called the conclusion (or consequence).
"if $p$, then $q$ "
"if $p, q$ "
" $p$ is sufficient for $q$ "
" $q$ if $p$ "
" $q$ when $p$ "
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| TABLE 5 The Truth Table for the Conditional Statement$p \rightarrow q .$ |  |  |
| :---: | :---: | :---: |
| $p$ | $q$ | $p \rightarrow q$ |
| T | T | T |
| T | F |  |
| F | T | T |
| F | F | T |

" $p$ implies $q$ "
" $p$ only if $q$ "
"a sufficient condition for $q$ is $p$ "
" $q$ whenever $p$ "
" $q$ is necessary for $p$ "
" $q$ follows from $p$ "

## Compound Propositions (11/23)

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## Logical Connectives

EXAMPLE 1
"If you get $100 \%$ on the final, then you will get an A."

If you manage to get a $100 \%$ on the final, then you would expect to receive an A. If you do not get $100 \%$ you may or may not receive an A depending on other factors. However, if you do get $100 \%$, but the professor does not give you an A, you will feel cheated.

## Compound Propositions (12/23)

## كلية الحاسبات والذكاء الإصطناعي

## Logical Connectives

EXAMPLE 2
Let $p$ be the statement "Maria learns discrete mathematics" and $q$ the statement "Maria will find a good job." Express the statement $p \rightarrow q$ as a statement in English.

## Compound Propositions (12/23)

## كلية الحاسبات والذكاء الإصطناعي

## Logical Connectives

## EXAMPLE 2

Let $p$ be the statement "Maria learns discrete mathematics" and $q$ the statement "Maria will find a good job." Express the statement $p \rightarrow q$ as a statement in English.
"If Maria learns discrete mathematics, then she will find a good job."
"Maria will find a good job when she learns discrete mathematics."

## Compound Propositions (13/23)

## كلية الحاسبات والذكاء الإصطناعي

## Logical Connectives

EXAMPLE 3
"If today is Friday, then $2+3=6$."

## Compound Propositions (13/23)

## Logical Connectives

EXAMPLE 3
"If today is Friday, then $2+3=6$."
is true every day except Friday, even though $2+3=6$ is false.

## Compound Propositions (14/23)

## Logical Connectives

## DEFINITION 6

Let $p$ and $q$ be propositions. The biconditional statement $p \leftrightarrow q$ is the proposition " $p$ if and only if $q$." The biconditional statement $p \leftrightarrow q$ is true when $p$ and $q$ have the same truth values, and is false otherwise. Biconditional statements are also called bi-implications.

| TABLE 6 The Truth Table for the <br> Biconditional $\boldsymbol{p} \leftrightarrow \boldsymbol{q}$. |  |  |  |
| :---: | :---: | :---: | :---: |
| $\boldsymbol{p}$ | $\boldsymbol{q}$ | $\boldsymbol{p} \leftrightarrow \boldsymbol{q}$ |  |
| T | T | T |  |
| T | F | F |  |
| F | T | F |  |
| F | F | T |  |

"You can take the flight if and only if you buy a ticket."

## Compound Propositions (15/23)

## Truth Tables of Compound Propositions

example 1
Construct the truth table of the compound proposition $(p \vee \neg q) \rightarrow(p \wedge q)$.

## Compound Propositions (16/23)

## Truth Tables of Compound Propositions

example 1
Construct the truth table of the compound proposition
$(p \vee \neg q) \rightarrow(p \wedge q)$.

| TABLE 7 The Truth Table of $(p \vee \neg q) \rightarrow(p \wedge q)$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $p$ | $q$ | $\neg q$ | $p \vee \neg q$ | $p \wedge q$ | $(p \vee \neg q) \rightarrow(p \wedge q)$ |
| T | T |  |  |  |  |
| T | F |  |  |  |  |
| F | T |  |  |  |  |
| F | F |  |  |  |  |

## Compound Propositions (16/23)

## Truth Tables of Compound Propositions

example 1
Construct the truth table of the compound proposition
$(p \vee \neg q) \rightarrow(p \wedge q)$.

| TABLE 7 The Truth Table of $(p \vee \neg q) \rightarrow(p \wedge q)$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $p$ | $q$ | $\neg q$ | $p \vee \neg q$ | $p \wedge q$ | $(p \vee \neg q) \rightarrow(p \wedge q)$ |
| T | T | F |  |  |  |
| T | F | T |  |  |  |
| F | T | F |  |  |  |
| F | F | T |  |  |  |

## Compound Propositions (16/23)

## Truth Tables of Compound Propositions

example 1
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$(p \vee \neg q) \rightarrow(p \wedge q)$.

| TABLE 7 The Truth Table of $(p \vee \neg q) \rightarrow(p \wedge q)$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $p$ | $q$ | $\neg q$ | $p \vee \neg q$ | $p \wedge q$ | $(p \vee \neg q) \rightarrow(p \wedge q)$ |
| T | T | F | T |  |  |
| T | F | T | T |  |  |
| F | T | F | F |  |  |
| F | F | T | T |  |  |

## Compound Propositions (16/23)

## Truth Tables of Compound Propositions

example 1
Construct the truth table of the compound proposition
$(p \vee \neg q) \rightarrow(p \wedge q)$.

| TABLE 7 The Truth Table of $(\boldsymbol{p} \vee \neg q) \rightarrow(p \wedge q)$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{p}$ | $\boldsymbol{q}$ | $\neg \boldsymbol{q}$ | $\boldsymbol{p} \vee \neg \boldsymbol{q}$ | $\boldsymbol{p} \wedge q$ | $(p \vee \neg q) \rightarrow(p \wedge q)$ |
| T | T | F | T | T |  |
| T | F | T | T | F |  |
| F | T | F | F | F |  |
| F | F | T | T | F |  |

## Compound Propositions (16/23)

## Truth Tables of Compound Propositions

example 1
Construct the truth table of the compound proposition $(p \vee \neg q) \rightarrow(p \wedge q)$.

| TABLE 7 The Truth Table of $(\boldsymbol{p} \vee \neg \boldsymbol{q}) \rightarrow(\boldsymbol{p} \wedge \boldsymbol{q})$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{p}$ | $\boldsymbol{q}$ | $\neg \boldsymbol{q}$ | $\boldsymbol{p} \vee \neg \boldsymbol{q}$ | $\boldsymbol{p} \wedge \boldsymbol{q}$ | $(\boldsymbol{p} \vee \neg \boldsymbol{q}) \rightarrow(\boldsymbol{p} \wedge \boldsymbol{q})$ |
| T | T | F | T | T | T |
| T | F | T | T | F | F |
| F | T | F | F | F | T |
| F | F | T | T | F | F |

## Compound Propositions (17/23)

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## Precedence of Logical Operators

| TABLE 8 <br> Precedence of <br> Logical Operators. |  |
| :---: | :---: |
| Operator | Precedence |
| $\neg$ | 1 |
| $\wedge$ | 2 |
| $\vee$ | 3 |
| $\rightarrow$ | 4 |
| $\leftrightarrow$ | 5 |

## Compound Propositions (18/23)

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## Truth Tables of Compound Propositions

EXAMPLE 2
Construct the truth table of the compound proposition $(p \wedge \neg q) \rightarrow r$

## Compound Propositions (19/23)

## Truth Tables of Compound Propositions

EXAMPLE 2
Construct the truth table of the compound proposition $(p \wedge \neg q) \rightarrow r$

| $p$ | $q$ | $r$ | $\neg q$ | $p \wedge \neg q$ | $(p \wedge \neg q) \rightarrow r$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
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## Compound Propositions (19/23)

## Truth Tables of Compound Propositions

EXAMPLE 2
Construct the truth table of the compound proposition $(p \wedge \neg q) \rightarrow r$

| $p$ | $q$ | $r$ | $\neg q$ | $p \wedge \neg q$ | $(p \wedge \neg q) \rightarrow r$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{T}$ | $\mathbf{T}$ | $\mathbf{T}$ |  |  |  |
| $\mathbf{T}$ | $\mathbf{T}$ | $\mathbf{F}$ |  |  |  |
| $\mathbf{T}$ | $\mathbf{F}$ | $\mathbf{T}$ |  |  |  |
| $\mathbf{T}$ | $\mathbf{F}$ | $\mathbf{F}$ |  |  |  |
| $\mathbf{F}$ | $\mathbf{T}$ | $\mathbf{T}$ |  |  |  |
| $\mathbf{F}$ | $\mathbf{T}$ | $\mathbf{F}$ |  |  |  |
| $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{T}$ |  |  |  |
| $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{F}$ |  |  |  |

## Compound Propositions (19/23)

## Truth Tables of Compound Propositions

EXAMPLE 2
Construct the truth table of the compound proposition $(p \wedge \neg q) \rightarrow r$

| $\boldsymbol{p}$ | $q$ | $r$ | $\neg q$ | $p \wedge \neg q$ | $(p \wedge \neg q) \rightarrow r$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{T}$ | $\mathbf{T}$ | $\mathbf{T}$ | $\mathbf{F}$ |  |  |
| $\mathbf{T}$ | $\mathbf{T}$ | $\mathbf{F}$ | $\mathbf{F}$ |  |  |
| $\mathbf{T}$ | $\mathbf{F}$ | $\mathbf{T}$ | $\mathbf{T}$ |  |  |
| $\mathbf{T}$ | $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{T}$ |  |  |
| $\mathbf{F}$ | $\mathbf{T}$ | $\mathbf{T}$ | $\mathbf{F}$ |  |  |
| $\mathbf{F}$ | $\mathbf{T}$ | $\mathbf{F}$ | $\mathbf{F}$ |  |  |
| $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{T}$ | $\mathbf{T}$ |  |  |
| $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{T}$ |  |  |

## Compound Propositions (19/23)

## Truth Tables of Compound Propositions

EXAMPLE 2
Construct the truth table of the compound proposition $(p \wedge \neg q) \rightarrow r$

| $p$ | $q$ | $r$ | $\neg q$ | $p \wedge \neg q$ | $(p \wedge \neg q) \rightarrow r$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{T}$ | $\mathbf{T}$ | $\mathbf{T}$ | $\mathbf{F}$ | $\mathbf{F}$ |  |
| $\mathbf{T}$ | $\mathbf{T}$ | $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{F}$ |  |
| $\mathbf{T}$ | $\mathbf{F}$ | $\mathbf{T}$ | $\mathbf{T}$ | $\mathbf{T}$ |  |
| $\mathbf{T}$ | $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{T}$ | $\mathbf{T}$ |  |
| $\mathbf{F}$ | $\mathbf{T}$ | $\mathbf{T}$ | $\mathbf{F}$ | $\mathbf{F}$ |  |
| $\mathbf{F}$ | $\mathbf{T}$ | $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{F}$ |  |
| $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{T}$ | $\mathbf{T}$ | $\mathbf{F}$ |  |
| $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{T}$ | $\mathbf{F}$ |  |

## Compound Propositions (19/23)

## Truth Tables of Compound Propositions

EXAMPLE 2
Construct the truth table of the compound proposition $(p \wedge \neg q) \rightarrow r$

| $p$ | $q$ | $r$ | $\neg q$ | $p \wedge \neg q$ | $(p \wedge \neg q) \rightarrow r$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{T}$ | $\mathbf{T}$ | $\mathbf{T}$ | $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{T}$ |
| $\mathbf{T}$ | $\mathbf{T}$ | $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{T}$ |
| $\mathbf{T}$ | $\mathbf{F}$ | $\mathbf{T}$ | $\mathbf{T}$ | $\mathbf{T}$ | $\mathbf{T}$ |
| $\mathbf{T}$ | $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{T}$ | $\mathbf{T}$ | $\mathbf{F}$ |
| $\mathbf{F}$ | $\mathbf{T}$ | $\mathbf{T}$ | $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{T}$ |
| $\mathbf{F}$ | $\mathbf{T}$ | $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{T}$ |
| $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{T}$ | $\mathbf{T}$ | $\mathbf{F}$ | $\mathbf{T}$ |
| $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{F}$ | $\mathbf{T}$ | $\mathbf{F}$ | $\mathbf{T}$ |

## Compound Propositions (20/23)

## Logic and Bit Operations

- Computers represent information using bits. A bit is a symbol with two possible values, namely, 0 (zero) and 1 (one).



## Compound Propositions (21/23)

## Computer Bit Operations

- We will also use the notation OR, AND, and XOR for the operators $\vee, \wedge$, and $\oplus$, as is done in various programming languages.

TABLE 9 Table for the Bit Operators $\boldsymbol{O R}$, $A N D$, and $X O R$.

| $\boldsymbol{x}$ | $\boldsymbol{y}$ | $\boldsymbol{x} \vee \boldsymbol{y}$ | $\boldsymbol{x} \wedge \boldsymbol{y}$ | $\boldsymbol{x} \oplus \boldsymbol{y}$ |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 | 1 |
| 1 | 0 | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 | 0 |

## Compound Propositions (22/23)

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## Bit Strings

- Information is often represented using bit strings, which are lists of zeros and ones. When this is done, operations on the bit strings can be used to manipulate this information.

A bit string is a sequence of zero or more bits. The length of this string is the number of bits in the string.

```
101010011 is a bit string of length nine.
```


## Compound Propositions (23/23)

## Example

- Find the bitwise OR, bitwise AND, and bitwise XOR of the bit strings 0110110110 and 1100011101

0110110110<br>1100011101<br>1110111111 bitwise $O R$<br>0100010100 bitwise AND<br>1010101011 bitwise XOR

## Video Lectures

All Lectures: https://www.youtube.com/playlist?list=PLx|vc-MGCsGgZIMVY

## Lecture \#|: https://www.youtube.com/watch?v=eFDzhnilnc48list=PLxlvcMEDsEqZIMVY

https://www.youtube.com/watch?v=dCZBBam4BksClist=PLx|vcMEDsBgZIMVYOEEtUHUImfUquLjiwzZindex=2
https://www.youtube.com/watch?v=-BxvBFJaNGE\&list=PLxlvcMEDsEgZIMVYOEEtUHUmfUquLjiwzZiindex=3

## Thank You

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